

Figure S1: Biplots of phylogenetically-corrected Principal Component Analysis for observations of foraging behavior in honeyeater species. Species names are given at their PC value coordinates. PC loadings for each foraging variable are described as arrows.


Figure S2: Warp grids illustrating the extremes of beak shape PC axis 3, which is described in the text as "tapering".


Figure S3: Phylogenetically-corrected path analyses were repeated using body size as a covariate. Format follows Figure 2. Model fit is assessed by the C -statistic information criterion (CICc) following [61]. The best fitting model is shown in (e), with red arrows indicating negative associations and blue arrows indicating positive ones; values shown below each arrow refer to correlation coefficients.


Figure S4: Effect size forest plot for total effect estimates from the phylogenetically-corrected path analysis described in Figure 2 e . Error bars describe $95 \%$ confidence intervals around standardized regression coefficients. Abbreviations are as follows: Nect, Foraging pPC1; WminT, Winter Minimum Temperature; SmaxT, Summer Maximum Temperature; Depth, Beak Shape PC1; Curve, Beak Shape PC2; Size, Beak Centroid Size.


Polynomial Regression Model
Beak Shape PC3


Polynomial Regression Model
Beak Size


Polynomial Regression Model
Beak Shape PC1


Polynomial Regression Model
Beak Shape PC3


Polynomial Regression Model
Beak Size


Figure S5: Polynomial regression models for the effect of winter and summer temperatures on beak shape and size. Model fitting was performed in multivariate, phylogenetically corrected framework, and relevant terms of best fitting models are shown here.

Epthianura
tricolor



Philemon buceroides


5 mm


(abbreviated 1/2)

Figure S6: Comparison of extreme beak sizes and the songs those species perform. The Crimson Chat Epthianura tricolor is Australia's smallest honeyeater and performs a high trill, whereas the Helmeted Friarbird Philemon buceroides is Australia's largest honeyeater and performs a series of long whistles. Scale bars are shown for beak length (mm), time (seconds), and frequency (Hz).


Figure S7: Forest plot for PGLS analysis results describing the effect of beak size and shape on song pace. Since beak size and body size are tightly correlated, we avoided including both as covariates. Here we repeat the analysis described in Figure 4a, panel 1 using body size rather than beak size.

TableS1. PCA loadings of ecological data describing dietary preferences and foraging behavior of honeyeater species, based on observations by ET Millerand SK Wagner (Milleretal. 2017). Foreach PCaxis, descriptions are given for the threefactors with the greatestabsolute PCloadings. The firstfour PCaxes togetheraccountfor a cumulative $47 \%$ of the total variance.

| PC1 | Loading | PC2 | Loading | PC3 | Loading | PC4 | Loading |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Gleaning | 0.86 | Mean \% Canopy | 0.71 | Pulling | -0.64 | Reaching | 0.61 |
| Air | -0.73 | Mean Third | -0.69 | Gaping | -0.73 | Woody Fruits | -0.64 |
| Nectarivory | -0.87 | Ground | -0.93 | Hanging Bark | 0.75 | InsectCases | -0.68 |

Table S2: Results of multivariate phylogenetic generalized least squares (PGLS) regressions conducted with each beak morphology response variable. Effect sizes and their standard errors are reported in terms of standardized beta regression coefficients.

| Response Variable | Predictor Variable | Effect Size (std. B) | ES (std. err.) | $t$ value | P value |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Beak PC1 | Foraging PC1 (17\%) | 0.485 | 0.101 | 4.785 | 0.000 |
| (Depth) | Foraging PC2 (13\%) | -0.046 | 0.121 | -0.379 | 0.706 |
|  | Foraging PC3 (10\%) | 0.133 | 0.073 | 1.811 | 0.075 |
|  | Foraging PC4(8\%) | 0.109 | 0.084 | 1.299 | 0.199 |
|  | Summermax T | 0.169 | 0.092 | 1.836 | 0.071 |
|  | Wintermin T | -0.308 | 0.092 | -3.333 | 0.002 |
|  | Body Mass | 0.110 | 0.097 | 1.140 | 0.259 |
| Beak PC2 | Foraging PC1 | 0.408 | 0.106 | 3.851 | 0.000 |
| (Curvature) | Foraging PC2 | -0.114 | 0.124 | -0.919 | 0.362 |
|  | Foraging PC3 | -0.122 | 0.089 | -1.373 | 0.175 |
|  | Foraging PC4 | -0.382 | 0.093 | -4.116 | 0.000 |
|  | Summermax T | -0.264 | 0.113 | -2.331 | 0.023 |
|  | Wintermin T | -0.024 | 0.105 | -0.231 | 0.818 |
|  | Body Mass | 0.043 | 0.102 | 0.419 | 0.677 |
| Beak PC3 | Foraging PC1 | 0.148 | 0.124 | 1.196 | 0.236 |
| (Tapering) | Foraging PC2 | 0.442 | 0.146 | 3.020 | 0.004 |
|  | Foraging PC3 | 0.238 | 0.099 | 2.401 | 0.019 |
|  | Foraging PC4 | -0.206 | 0.106 | -1.937 | 0.057 |
|  | Summermax T | 0.059 | 0.127 | 0.464 | 0.644 |
|  | Wintermin T | -0.265 | 0.120 | -2.211 | 0.031 |
|  | Body Mass | -0.110 | 0.120 | -0.921 | 0.361 |
| Beak Size | Foraging PC1 | -0.314 | 0.078 | -4.038 | 0.000 |
|  | Foraging PC2 | -0.033 | 0.095 | -0.345 | 0.731 |
|  | Foraging PC3 | -0.080 | 0.055 | -1.453 | 0.151 |
|  | Foraging PC4 | -0.045 | 0.064 | -0.696 | 0.489 |
|  | Summermax T | -0.073 | 0.067 | -1.089 | 0.280 |
|  | Wintermin T | 0.289 | 0.070 | 4.098 | 0.000 |
|  | Body Mass | 0.567 | 0.075 | 7.572 | 0.000 |

Table S3: Results of AIC model fit comparisons among multivariate phylogenetic generalized least squares (PGLS) regressions conducted with polynomial temperature

| Response Variable | Summer max T | Winter min T | delta AIC |
| :---: | :---: | :---: | :---: |
| Beak PC1 | Linear | 3rd Order | 0.0 |
| (Depth) | 3rd Order | 3rd Order | 2.8 |
|  | Linear | 2nd Order | 4.1 |
|  | 2nd Order | 2nd Order | 6.0 |
|  | Linear | Linear | 9.1 |
|  | 2nd Order | Linear | 10.3 |
|  | 3rd Order | Linear | 12.1 |
| Beak PC2 | Linear | Linear | 0.0 |
| (Curvature) | Linear | 2nd Order | 1.2 |
|  | 2nd Order | Linear | 1.4 |
|  | Linear | 3rd Order | 2.7 |
|  | 3rd Order | Linear | 2.7 |
|  | 2nd Order | 2nd Order | 4.3 |
|  | 3rd Order | 3rd Order | 5.7 |
| Beak PC3 | 3rd Order | 3rd Order | 0.0 |
| (Tapering) | 2nd Order | 2nd Order | 2.5 |
|  | 2nd Order | Linear | 3.8 |
|  | 3rd Order | Linear | 5.1 |
|  | Linear | 2nd Order | 5.8 |
|  | 3rd Order | Linear | 6.4 |
|  | Linear | Linear | 6.4 |
| Beak Size | 3rd Order | 3rd Order | 0.0 |
|  | 3rd Order | Linear | 4.7 |
|  | 2nd Order | 2nd Order | 6.5 |
|  | 2nd Order | Linear | 7.5 |
|  | Linear | 3rd Order | 9.9 |
|  | Linear | Linear | 13.2 |
|  | Linear | 2nd Order | 14.8 |

