

Supplementary materials

featuring article

Limits to the rate of information transmission through MAPK pathway

by

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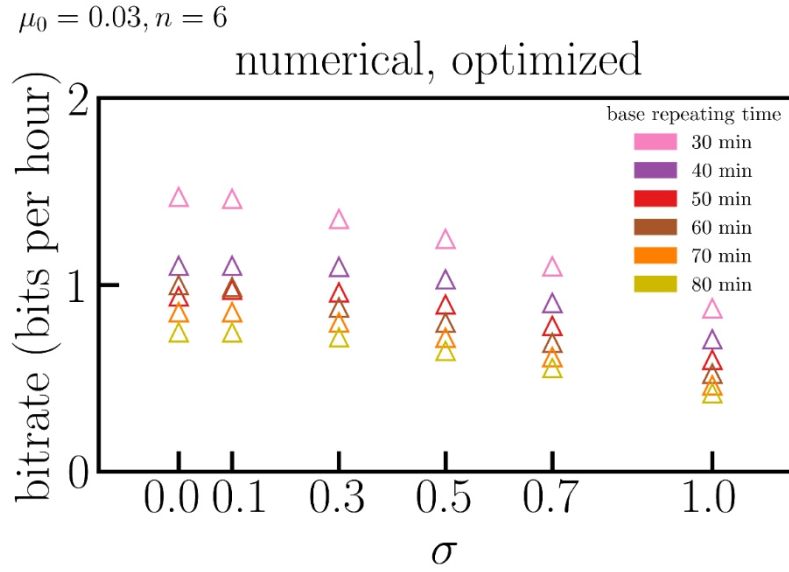
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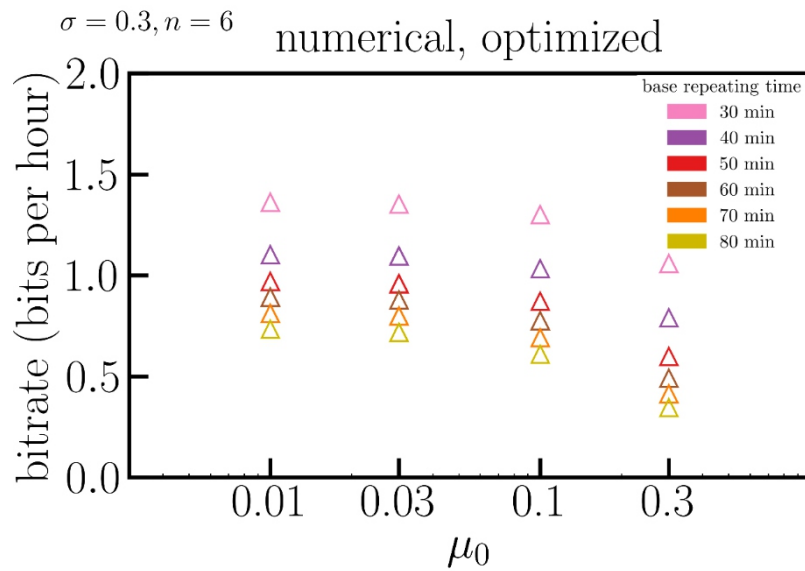
Supplementary Figure 1. Influence of extrinsic noise on transmitted information.

Supplementary Figure 2. Influence of additive noise on transmitted information.

Supplementary Table 1. Parameter values for the MAPK pathway model.



Supplementary Figure 1. Influence of cell specific noise on transmitted information. Mutual information was calculated numerically as follows: triangles – maximized, circles – assuming equal probabilities of all group representatives, squares – assuming equal probabilities of all input sequences.



Supplementary Figure 2. Influence of additive noise on transmitted information. Mutual information was calculated numerically as follows: triangles – maximized, circles – assuming equal probabilities of all group representatives, squares – assuming equal probabilities of all input sequences.

Supplementary Table 1. Parameter values for the MAPK pathway model.

Default values originate from the article by Kočańczyk *et al.* (2017), *Sci. Rep.*, 7:38244, doi:10.1038/srep38244.

The parameters of the pathway that are drawn from the lognormal distribution $\text{LogN}(\mu_i, \sigma)$ are written in bold green.

Parameter	Description
<i>Concentrations (protein copy number per cell)</i>	
EGFR_{tot} = 3×10^5	Total number of EGFR molecules
RAS_{tot} = 6×10^4	Total number of RAS molecules
SOS_{tot} = 10^5	Total number of SOS molecules
RasGAP_{tot} = 6×10^3	Total number of RasGAP molecules
RAF_{tot} = 5×10^5	Total number of RAF molecules
MEK_{tot} = 2×10^5	Total number of MEK molecules
ERK_{tot} = 3×10^6	Total number of ERK molecules
<i>Rate constant for fast processes (s⁻¹)</i>	
$k_{\text{fast}} = 100$	As a simplification, three (pseudo) first-order processes considered in the model are assumed to be fast.
<i>Rate constants for activation processes [(molecules/cell)⁻¹ s⁻¹ except (pg/ml)⁻¹ s⁻¹ for a_1]</i>	
$a_1 = 5 \times 10^{-5}$	EGF-mediated activation of EGFR
$a_2 = 10^{-7}$	Activation of RAF by RAS-GTP
$b_1 = 10^{-5}$	Binding of EGF-activated EGFR and dephosphorylated SOS
$p_1 = 10^{-7}$	Phosphorylation of MEK's activation sites by RAF
$p_2 = 3 \times 10^{-6}$	Phosphorylation of ERK's activation sites by MEK
<i>Rate constants for deactivation processes (s⁻¹)</i>	
$d_1 = d = 0.01$	Deactivation of EGFR
$d_2 = d$	Deactivation of RAF (spontaneous)
$u_{1A} = d$	Dissociation of active EGFR–SOS complex
$q_1 = d$	Dephosphorylation of MEK's activation sites
$q_2 = d$	Dephosphorylation of ERK's activation sites
<i>Rate constants for SOS association reactions [(molecules/cell)⁻¹ s⁻¹] and dissociation reactions (s⁻¹)</i>	

$b_{2A} = 10^{-6}$	Association of SOS and RAS-GTP
$b_{2B} = 0.1 \times b_{2A}$	Association of SOS and RAS-GDP
$u_{1B} = k_{\text{fast}}$	Dissociation of inactive EGFR–SOS complex
$u_{2A} = u_{2B} = 1$	Dissociation of SOS–RAS-GTP complex and SOS–RAS-GDP complex
<i>Rate constants associated with SOS-to-RAS positive feedback [(molecules/cell)⁻¹ s⁻¹ except s⁻¹ for k_3 and u_3]</i>	
$k_{2A} = 10^{-4}$	SOS's nucleotide-exchange activity when RAS-GTP is bound to its REM domain
$k_{2B} = 0.1 \times k_{2A}$	SOS's nucleotide-exchange activity when RAS-GDP is bound to its REM domain
$k_{2C} = 0$	SOS's nucleotide-exchange activity when no RAS is bound to its REM domain
$b_3 = 10^{-5}$	Association of RasGAP and RAS-GTP
$k_3 = k_{\text{fast}}$	RasGAP-facilitated RAS-GTP→RAS-GDP hydrolysis
$u_3 = 0.01$	Dissociation of RasGAP from RAS-GDP after hydrolysis of GTP
<i>Rate constants associated with ERK-mediated negative feedbacks [(molecules/cell)⁻¹ s⁻¹]</i>	
$p_3 = 3 \times 10^{-9}$	Phosphorylation of unbound SOS by active ERK
$p_4 = p_6 = p = 6 \times 10^{-10}$	Phosphorylation of MEK (T292 in MEK1) and RAF by active ERK
<i>Rate constants for (spontaneous) dephosphorylation reactions (s⁻¹)</i>	
$q_3 = q_4 = q_6 = q = 3 \times 10^{-4}$	Dephosphorylation of inhibitory phosphosites in SOS, MEK (T292 in MEK1), RAF
$q_5 = k_{\text{fast}}$	Dephosphorylation of MEK's activation sites when MEK's T292 is phosphorylated
<i>ERK activity reporters – concentrations (protein copy number per cell)</i>	
$\text{EKAR3}_{\text{tot}} = \text{ERKTR}_{\text{tot}} = 10^6$	Total number of EKAR3 and ERKTR molecules
<i>ERK activity reporters – rate constants for activation reactions [(molecules/cell)⁻¹ s⁻¹]</i>	
$a_{\text{EKAR3}} = 3 \times 10^{-9}$	EKAR3 activation rate by active ERK
$a_{\text{ERKTR}} = 10^{-9}$	ERKTR activation rate by active ERK
<i>ERK activity reporters – rate constants for deactivation reactions (s⁻¹)</i>	
$d_{\text{EKAR3}} = 10^{-3}$	EKAR3 deactivation rate