**The Tradeoff Between Fertility and Predation Risk Drives a Geometric Sequence in the Pattern of Group Sizes in Baboons**

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**Supplementary Information**

***Supplementary Methods***

*Data*

We take group (or troop) size to be that defined by the field worker: in most cases, this grouping is fairly obvious, since baboons forage and sleep together in stable social groups that maintain a degree of demographic coherence and stability over time, as well as clear spatial separation between neighbouring groups. Exactly what counts as a group in *Papio papio* has been the subject of some debate because of this species’ apparently more flexible form of sociality, but all field workers on this species agree on the existence of some form of stable social group, at least as defined by animals that share a common range area (Dunbar & Nathan 1972; Boese 1975; Sharman 1981; Patzelt et al. 2011). Again, we simply use the group as defined by the fieldworker concerned. Rather than biasing results, differences in definition will always have the effect of increasing error variance, and hence will bias in favour of the null hypothesis, thus reducing the likelihood of finding any consistent patterns.

All group sizes are either based on censuses on a particular date or an average across a study period, as specified in the original study. In populations that were subject to long term study (more than a single year) with repeated censuses of the same social groups, we counted a census as being new only providing it had been carried out at least five years after the previous census of that group. In either case, we always used the original (i.e. earliest) census and at most one later census. The data are provided in *Supplementary Dataset1.*

In most cases, fertility rates are based on observed mean birth rate or mean interbirth interval for a single social group, as specified in the original publications. For the two Guinea baboon (*Papio papio*) samples, birth rates were estimated from the number of immatures per female, averaged across several groups, for each of the two study sites (Boese 1975, pers. comm.; Sharman 1981). In these two cases, each group was censussed just once, with the sample based on a large number of troops (13 and 17, respectively). Immatures are defined as animals that are pre-puberty, with puberty occurring at around 4 years of age (Altmann et al. 1977). Juvenile mortality will inevitably lead to some underestimation of the true birth rate. However, since both newborns and older juveniles are included, the degree of underestimate will be lessened (the effective mortality rate will be half that experienced by animals that reach puberty). More importantly, other studies indicate a good correlation between fertility measured in this way and actual birth rates (Dunbar 2017). It should be noted, however, that we do not rely on these particular datapoints to determine the pattern observed in baboon fertility, but rather include them for completeness so as to be able to place *P. papio* into the comparative context. The pattern remains the same whether or not we include the *P. papio* data. The data are given in *Supplementary Dataset2*.

*Analysis*

We used maximum-likelihood methods (Clauset et al. 2009) to fit a set of common distributions (power law, truncated power law, geometric, negative binomial, exponential, stretched exponential, normal, lognormal, and a compound Poisson distribution), using the discrete approach as described by Clauset et al. (2009). We numerically maximised the log-likelihood of each candidate distribution to obtain its parameter estimates, using the *optimize* module of Python's *scipy* (v0.17.1) library. We identified the most likely model using AIC. Because models with more parameters are always more likely to fit the data, we applied the Jenks natural breaks clustering algorithm (Jenks 1967) to see if a different approach gives the same result. In order to choose the optimal number of clusters in this case, we calculated a goodness of fit for successive numbers of clusters and take a value of 0.85 as the threshold (following the recommendation by Coulson 1987).

The code for running MLE and Jenks can be obtained here:

<https://github.com/pmaccarron/clustering_methods>

Note that the Jenks implementation was developed in Python by Matthew Perry and can be found here: <https://github.com/perrygeo/jenks>

***Supplementary Results***

*Group size*

Table S1 gives the cluster means (and the mean scaling ratio between successive clusters) determined by the two clustering methods. These are in close agreement. The MLE data are based on the four Poisson distributions identified as the best fit to the data (see Table 1). The Jenks algorithm identified four clusters as optimal. In both cases, the scaling ratio approximates 2, indicating that it is likely to be underpinned by some kind of binary fission process.

*Table S1. Cluster means and mean scaling ratios between successive clusters generated by the two algorithms.*

Species Cluster means Mean

scaling ratio

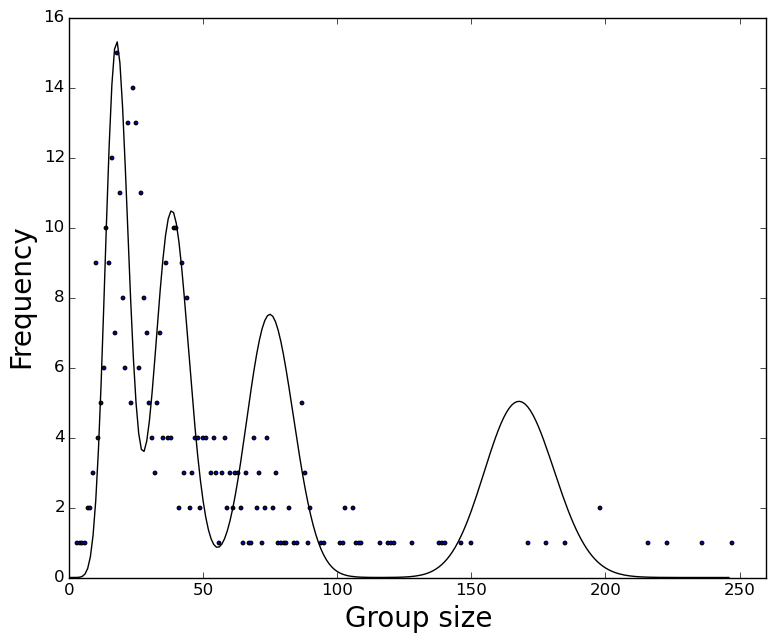
MLE 18.2 38.8 75.4 168.2 2.10

Jenks 19.9 45.4 85.5 183.2 2.10

Mean 19.1 42.1 80.5 175.7 2.10

Number of groups\* 202 132 61 14

\* Number of groups assigned to the cluster by the algorithms.



*Figure S1*

*Distribution of individual group sizes, overlain by the four theoretical cluster distributions generated by the cluster analysis.*

Fig. S2 plots the four Poisson distributions on the distribution of actual group sizes for the sample.

We checked the distribution of group sizes for each baboon species separately (Table S2). The Jenks algorithm identified either three or four clusters as optimal in each case, with cluster means that are very close to those observed in the sample as a whole (Table S1). Note that, in the case of *P. ursinus*, the means for clusters 3 and 4 actually straddle the overall mean for cluster 3 for the sample as a whole, with a combined mean of 80.4 (N=18) and a mean scaling ratio of 2.13. The distinction between them might be, thus, somewhat arbitrary.

These data confirm that a pattern of four clusters is characteristic of all four species with broadly similar mean values (albeit with some species missing the smallest or largest cluster), and is not simply a difference between species. *Papio anubis* does not have any groups in the largest cluster (~160) and *Papio papio* lacks groups in the smallest cluster (~20). All have scaling ratios between successive cluster means that approximate 2.

*Table S2. Optimal number of clusters, and the resulting cluster means and mean scaling ratios between successive clusters, for each of the species separately, compared to that for the pooled sample, using the Jenks algorithm.*

Species Cluster means \* Mean

scaling ratio

**All *Papio* 19.9 (202) 45.4 (132) 85.5 (61) 183.2 (14) 2.10**

*P. anubis* 22.2 (58) 49.3 (33) 94.1 (13) 2.06

*P. cynocephalus* 20.7 (32) 46.6 (41) 80.0 (28) 176.0 (4) 2.06

*P. ursinus* 17.8 (99) 37.1 (49) 64.9 (10) 99.8 (8) 1.79

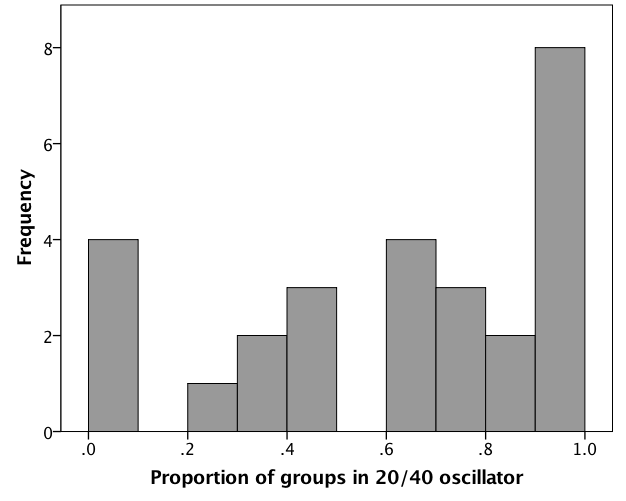
*P. papio* 42.0 (19) 113.0 (9) 216.3 (6) 2.30

\* Numbers in parentheses in the body of the table are the number of groups assigned to the cluster by the algorithm.

*The oscillator adopted is population-specific*

To determine whether individual populations have groups in all oscillators or exhibit a preference for one oscillator over the others, we first determined whether the distribution of group sizes at each sample site was normally distributed or not, and then which oscillator the mean concerned lies within. Of the 25 sites with a sample large enough to test (N≥5 groups), 20 were normally distributed (Kolmogorov-Smirnov one-sample tests against a normal distribution, p>0.05). In general, then, most sites have a characteristic group size with a single modal value. Of the 5 non-normal populations, two (Giant’s Castle and Nairobi Park) were bimodal within the same oscillator; the other three (Amboseli Park, Gilgil and Mt Assirik) were all essentially unimodal with a small number of outliers of groups with >100 animals. If groups >100 are excluded, these three are all normally distributed around a single modal value.

To determine how these means relate to the oscillators, we plot the proportion of groups in the smaller (20-40) oscillator in each population (treating the two larger oscillators as one, since the number of groups in the 80/160 grouping is very small) (Figure S2). The data fall naturally into two clusters: those with most or all their groups in the 20/40 oscillator and those with most or all of their groups within the 40/80 and 80/120 oscillators. No populations exhibit a completely even split. Indeed, both subsets have the kind of bimodal distribution that would be expected from an imperfect statistical process: some groups from the 20/40 oscillator set take longer to fission than they ideally should, and some groups in the 40/80 oscillator set fission unequally and sometimes produce daughter groups that are smaller than ideal.

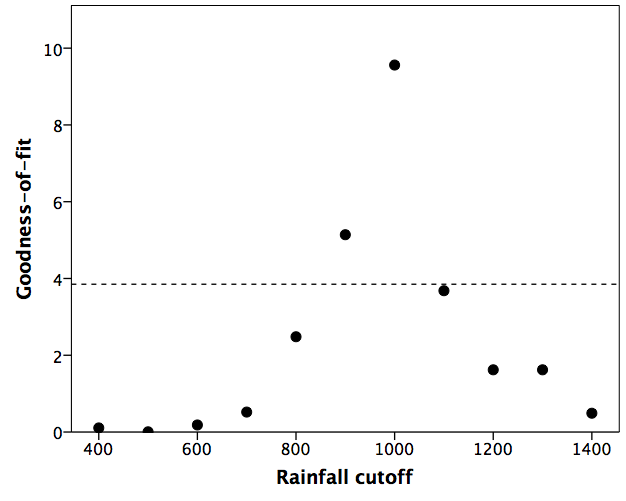


*Figure S2*

*Proportion of groups that fall into the lower (20-40) oscillator for 19 populations with N>4 groups sampled. Source: ESM Dataset S1*

*Identifying the transition point*

We interpret the distribution of group sizes, and the data in Fig. 1(b), as switch points between successive oscillators. In order to establish whether, and exactly where, there is a transition point in the distribution of group sizes in Fig. 1(b), we calculated the goodness of fit (χ2) for the number of datapoints below and above a group size of 40 at different rainfall cutoff values. Fig. S3 plots the respective values of χ2. Only cutoffs between approximately 850-1090mm yield a significantly non-random distribution; that at 1000mm yields a clear maximum, suggesting that ~1000mm identifies a transition point between the two oscillators.



*Figure S3*

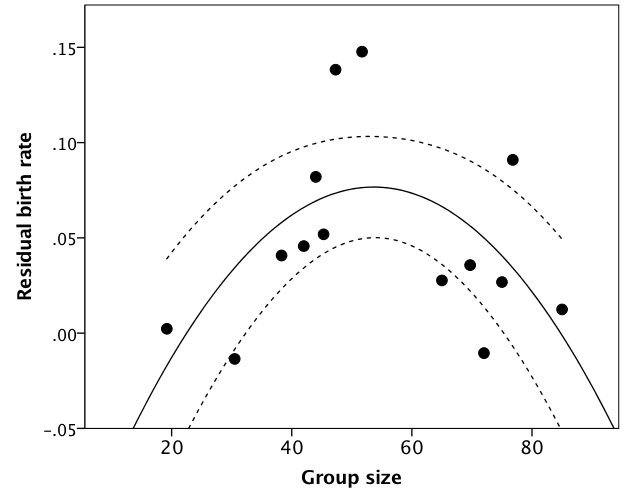
*Goodness-of-fit of the datapoints in Fig. 1(b) to a random distribution with the observed proportion below versus above a group size of 40 as a function of different rainfall cutoff values. The horizontal dashed line marks the minimum value of* χ2 for statistical significance (p=0.05 with df=1).

*Fertility*

The best-fit equation to the data in Fig. 2(a) is: b=0.097+0.0148N-0.000128N2 (where b = annual birth rate per female and N = group size).

The quadratic relationship between birth rate and group size in Fig. 2(a) holds individually across the three species for which there are sufficient datapoints to run a regression. Although the regressions are not individually significant, all are quadratic in the same direction (*P. anubis*: F1,2=0.02, p=0.979; *P. cynocephalus*: F2,2=12.18, p=0.076; *P. ursinus*: F2,3=7.08, p=0.073; all linear regressions, 0.875≥p≥0.317). Taken together, this set of equations is significantly more positively quadratic than would be expected if there were no underlying trend (Fisher’s meta-analysis for a directional hypothesis: χ2=14.59, df=6, p=0.024).

Hill et al. (2000) reported that baboon fertility is independently predicted by both the number of adult females in the group and the mean ambient temperature of the habitat (a reliable index of habitat quality). Mean annual temperature and group size are not correlated in our fertility sample (rs=-0.10, N=15, p=0.723). Nonetheless, to check whether environmental conditions might be a confound in our results, we regressed birth rate on mean habitat ambient temperature as a quadratic relationship (BirthRate = -0.672 + 0.104\*Temp - 0.00231\*Temp2: F2,18=3.77, r2=0.296, p=0.043; linear: F1,19=0.01, r2=0.000, p=0.933), and calculated residual birth rates from this regression. The results (Fig. S4) are identical to those shown in Fig. 2(a).



*Figure S4*

*Residual of mean birth rate regressed on mean local temperature plotted against group size for individual baboon groups.*

*Table S3. Backwards stepwise regression analysis of birth rate as a function of group size and temperature and their respective squared values.*

Model parameters r2 adj F df p AICc

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Group + Group2 0.654 13.31 2,11 0.001 -132.07

Group + Group2 + Temp 0.621 8.10 3,10 0.005 -129.63

Group + Group2 + Temp + Temp2 0.626 6.45 4,9 0.010 -127.03

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A backwards stepwise regression with both group size and temperature, and their squares, yields a best fit equation that has only group size and its square. The next best fit adds a linear effect of temperature, but the gain in fit is modest (Table S3). More importantly, a model comparison procedure using AIC identifies a model with just group size and its square as a significantly (ΔAIC>2) better fit than either of the alternative models. In sum, group size seems to be a more important determinant of fertility than habitat quality.

*Fertility and group size in mammals*

There is evidence that fertility declines with social group size in a taxonomically very wide range of mammals, including zebra (Pluháček et al. 2006), most canids (Moehlmann & Hofer 1997), hyaena (Holecamp et al. 1996), badgers (Woodroffe & MacDonald 1995), rodents (Huck et al. 1988; Kinahan & Pillay 2008, Wey et al. 2013), marmots (Downhower & Armitage 1971), mongoose (Creel et al. 1992) and meerkats (Young et al. 2006), as well as domestic stock (McClure 1968). Experimental studies of domestic stock indicate that stocking rate (i.e. social group size) is mainly responsible for this, independently of any impact that nutrition might have (von Borell et al. 2007; Einarsson et al. 2008; Dobson et al. 2012; Clarke 2014). Since the crucial factor underpinning the oscillator mechanisms seems to be widespread in mammals, it seems reasonable to expect that the same effects that we observe in baboons will be found in most other mammalian taxa.

*Optimal transition point between oscillators*

We model the reproductive payoffs that accrue when switching oscillator at different group sizes across the range of group sizes of interest (20-80 individuals). To do this, we use an average reproductive lifespan (age at first birth to age at maternal death) of 13 years (based on Bronikowski et al. 2002; Altmann & Alberts 2003; Cheney et al. 2004). Alternative choices of length of reproductive lifespan do not change the payoff ratios. We considered different pairs of oscillators across the range of group sizes 20-80 individuals, using switch points between the two oscillators varying between 25-75 in steps of 5. This gives us successive pairs of oscillators: 20-25 vs 25-80, 20-30 vs 30-80, 20-35 vs 35-80, etc. For each pair of oscillators, the female starts in a group of the lower value (i.e. for the 20/25 vs 25/80 pair, the female starts in a group of either 20 or 25, while in the 20/30 vs 30/80 pair she starts in a group of 20 or 30).

We summed the likelihood that a female would produce an infant (from Fig. 2a) in each successive year from the starting group size, allowing for the growth in group size as a result of births, and assuming that adult females account for 30% of total group size (a value that is typical of primates in general [Dunbar et al. 2018] and baboons in particular [Dunbar & MacCarron, in press]). For present purposes, we ignored mortality; since there is no evidence that mortality is strongly size-dependent, its effect will be constant and no advantage is gained by making the model unnecessarily complicated by including it.

When group size hits the ceiling defined by a given oscillator, the group undergoes fission and the female’s group reverts to the oscillator baseline (unless the ceiling is below 20, in which case in resets to 50% of the size at fission) since this is the smallest daughter group into which a group can partition and thus represents the worst case scenario. This cycle was repeated until the female ‘dies’. Our index is the ratio of payoffs to a female under the two conditions (i.e. oscillators). To make the presentation of the results more intuitive, we always use the larger payoff (fitness) as the denominator. The results are given in Fig. 2(b).

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